

Evidence of Additional Erroneous Enumerations from the Person Duplication Study

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A preliminary version of this paper, dated Oct. 26, 2001, was made available as a draft of an ESCAP II report, with a promise of a later revision. The current version is based on two rounds of comments from Census Bureau colleagues. New research is currently underway, and results from the new research will be reported when available.

The Census Bureau has decided to release this version of the paper, which has not received the full review process used for other ESCAP II reports, to clarify the findings of the Oct. 26 version. The report does not conform to the format of other ESCAP II reports, but it is being made available to inform outside researchers.

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ABSTRACT

In January 2001, the U.S. Census Bureau's coverage measurement survey of Census 2000, the Accuracy and Coverage Evaluation (A.C.E.), estimated a net census undercount of 3.3 million persons. The A.C.E. estimate of net census undercount incorporates estimates of census omissions and erroneous census enumerations. If the A.C.E. underestimates erroneous enumerations, it would tend to overstate the net undercount. One evaluation, the Measurement Error Reinterview (MER), estimates that the A.C.E. understates erroneous enumerations by 1.5 million, and a second, the person duplication study, implies that the A.C.E. misclassifies as correct approximately 2.1 million erroneous enumerations due to duplication.

To assess their overlap, the study files were merged. The merged results imply an A.C.E. underestimation of 2.6 million erroneous enumerations without allowance for duplicates missed by computer matching. When a uniform allowance for a 75.7% efficiency of computer matching at detecting duplicates is assumed, the additional undetected duplicates imply an A.C.E. underestimation of 2.9 million erroneous enumerations. An approximate calculation shows an implied change of roughly 3.2 million in the A.C.E. dual system estimate. The estimates using MER data make the same implicit assumptions about missing data, and investigation of these assumptions is a topic for future research. The discussion section notes several issues requiring investigation before A.C.E. estimates can be revised on the basis of these preliminary findings.

1. INTRODUCTION

By September 2001, three lines of investigation indicated or suggested that the Accuracy and Coverage Evaluation (A.C.E.) underestimated the number of erroneous enumerations in Census 2000. First, estimates from the Measurement Error Reinterview (MER) (Adams and Krejsa 2001) showed substantial underestimation of erroneous enumerations in the A.C.E. Second, a person duplication study based on computer matching of the A.C.E. E sample to census enumerations (Mule 2001) uncovered a large number of duplicates both to group quarters and to households beyond the A.C.E. search area. Comparison of these matched duplicates to their enumeration status in the A.C.E. (Feldpausch 2001a) indicated that the A.C.E. underestimated erroneous enumerations from these sources. Third, A.C.E. estimates of erroneous enumerations of persons living elsewhere on Census Day (April 1, 2000) dropped relative to the 1990 Post Enumeration Survey (Feldpausch 2001b). Although the historical comparison is the weakest of the three lines, the apparent drop is consistent with the other two lines of evidence that the A.C.E. underestimated erroneous enumerations.

Previous analyses of the MER and duplicate studies did not address the issue of their overlap. If the estimated erroneous enumerations based on both are simply added, their sum exceeds the

estimated net national undercount, 3.3 million persons, from the A.C.E. Logically, the duplication study only measures part of the erroneous enumerations in scope for the MER, so the large result implied by the duplication study suggested that the MER estimate may itself be an underestimate.

To assess their overlap, each study was first reviewed and to some extent re-analyzed. Files from the MER and duplication study were merged to permit an assessment of the overlap of the two studies. This approach permits an estimate of the underestimation of erroneous enumerations by the A.C.E. from the combined findings of the MER and duplicate studies. Figure 1 shows the interrelationship of the three duplicate studies. Table 1 summarizes the re-analysis and the combination of the studies in greater detail.

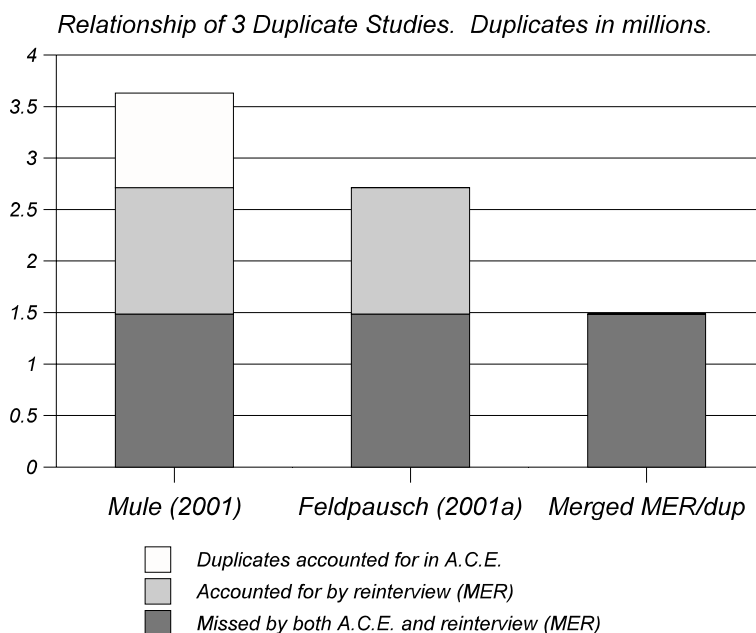


Fig. 1. Relationship of 3 duplicate studies. The duplicate study of Mule (2001) showed approximately 3.6M duplicates outside of the surrounding blocks or to group quarters, but this estimate includes (1) duplicates accounted for in the A.C.E. as erroneous enumerations elsewhere, (2) erroneous enumerations accounted for by the reinterview (MER) but not the A.C.E., and (3) duplicates missed by both the A.C.E. and MER. By matching the duplicate study to the A.C.E., Feldpausch (2001a) eliminated the effect of duplicates accounted for in A.C.E., but the resulting estimate of 2.7M overlaps with results from the MER. By merging the Feldpausch (2001a) and MER results, it is possible to estimate approximately 1.5M erroneous enumerations not found by the MER. All estimates are based on a presumed 75.7% efficiency for computer matching to find census duplicates.

Table 1 Summary of the merged MER/duplicate analysis. The EFU review of the MER produced an estimate of a net understatement of erroneous enumerations in the A.C.E. of 1,454,915. The estimate may be divided into a net underestimate of erroneous enumerations in the census of persons who should have been enumerated in group quarters on Census Day, and others, who were eligible for the E sample. Mule (2001) estimated the number of duplicates between the census and the E-sample eligible universe covered by the A.C.E. Results from the study suggest that computer matching may find only 75.7% of duplicates, and the primary analysis here incorporates an adjustment based on this rate. To assess the implications of the duplicates on A.C.E. estimates, Feldpausch (2001a) matched to the A.C.E. E-sample status to uncover duplicates not picked up by the A.C.E. The present study carries the approach one step further by merging the MER for the EFU review sample and the duplicate study to obtain estimates that may be combined with those from the MER/EFU review.

	Original Analysis	Re-analysis	Re-analysis with 75.7% Matching Efficiency	Integrated Analysis with 75.7% Matching Efficiency
MER/EFU review (Adams and Krejsa 2001)	1,454,915	1,454,915		1,454,915
E-sample eligible ^a		854,086		854,086
Group quarters ^b		600,829		600,829
Duplicate study (Mule 2001)	2,749,201	2,749,201	3,630,799	
E-sample eligible	2,089,107	2,089,107	2,759,030	
Group quarters	660,094	660,094	871,769	
Duplicates undetected by the A.C.E. E sample (Feldpausch 2001)		2,053,160	2,711,556	
E-sample eligible		1,555,090	2,053,767	
Group quarters	298,890	498,070	657,788	
Merged MER/duplicate studies		1,125,377	1,486,257	1,486,257
E-sample eligible		979,031	1,292,981	1,292,981
Group quarters		146,346	193,275	193,275
Total				2,941,172
E-sample eligible				2,147,067
Group quarters				794,104

Notes: a. "E-sample eligible" here refers to all sources of erroneous enumerations covered by the MER/EFU except group quarters.

b. Net of (1) review cases of A.C.E. correct enumerations reclassified as erroneous, living in group quarters, and (2) review cases of A.C.E. erroneous, living in group quarters, reclassified to correct enumerations in the review.

The MER was based on a reinterview sample drawn within about 1/5 of the sample clusters for the A.C.E. Interviews were conducted primarily in January and February 2001, during the Evaluation Followup (EFU). The original analysis of the MER, termed EFU 1, indicated an underestimation of erroneous enumerations by 1,919,029. To investigate whether the initial study was possibly flawed, a sample was selected from the MER for review by technical specialists under different and more specific coding procedures. No additional data was collected, but both the original A.C.E. data and the EFU interviews were recoded separately and then integrated into a Best Code. Adams and Krejsa (2001, pp. 3-4) revised the estimate of underestimation of erroneous enumerations from 1,919,029 to 1,454,915 (Table 1). The estimate 1,454,915 is itself the net of two estimates: 1,816,315 A.C.E. correct enumerations reclassified as erroneous and 361,400 A.C.E. erroneous reclassified as correct. Through a re-analysis of figures in their report, it is possible to separate the estimated 1,454,915 net error into approximately 600,829 persons who should have been enumerated in group quarters instead and 854,086 for other reasons (Table 1). (*Group quarters* includes both noninstitutional facilities such as college dormitories and military barracks; and institutions such as nursing homes, hospitals, jails, and prisons.)

The rates of missing data limit the interpretation of the MER. The unresolved rate for the EFU 1 analysis was 1.7%. The EFU review increased the unresolved rate for the Best Code to 4.8% and added a new category of Conflicting at 1.0%. The two estimates of 1,919,029 and 1,454,915 make similar implicit assumptions about the treatment of unresolved and conflicting cases, namely to retain the original A.C.E. status. Adams and Krejsa (2001, p. 15) provide a table showing a wide range of effects on the overall erroneous enumeration rate resulting from alternative assumptions about the erroneous enumeration rates for unresolved and conflicting cases.

Mule (2001) reported on the results of a computer match of the A.C.E. sample to the census, including group quarters. Census 2000 processing for the first time captured names and dates of birth from the forms. There were two stages of matching. The first was based on an exact match of name and date of birth. Census households were provisionally linked together whenever an exact match of one or more persons occurred between them. A second stage was based on statistical matching of any remaining persons in the provisionally linked households. Only some of the second-stage matches were retained as probable matches, on the basis of the similarity of the linked households. Additionally, some exact matches were evaluated under a model for coincidental agreement of birthday by persons with the same name to estimate a weight reflecting the probability that the match was the same person.

Comparison to A.C.E. results indicates that computer matching underestimates total duplication in the census. The A.C.E. estimated duplicates within cluster through clerical matching. Within cluster, computer matching yielded an estimate of only 724,687, 37.8% of the A.C.E. result (Mule 2001, p. 9). In a case-by-case comparison, computer matching discovered few duplicates missed by the clerks (*I*). An evaluation of the A.C.E. clerical work confirmed its high level of accuracy (Bean 2001, p. 22).

The A.C.E. also used clerical matching to estimate duplication to surrounding blocks in the *search area* (2) for some cases. Computer matching found an estimated 146,880 duplicates to surrounding blocks, somewhat higher than the A.C.E. result (3), which was based on searching surrounding blocks for only a subset of A.C.E. cases.

A.C.E. did not separately estimate duplicates beyond the search area. Instead, each duplicated person was assumed to regard at most one of these places as the correct residence on Census Day, and to regard the other enumeration as not the Census Day address. The A.C.E. questionnaire specifically attempted to identify persons counted at an incorrect address in order to include them in the estimated erroneous enumerations. Feldpausch (2001b, p. 21) adjusted the A.C.E. E-sample estimates to distribute the imputations for incomplete E-sample data into type of erroneous enumeration; her result implies approximately 3.73 million erroneous enumerations of persons at an incorrect address. This estimate includes not only duplicates beyond the search area but also erroneous enumerations of persons who were enumerated only once in the census but at an incorrect address.

Mule (2001, p. 11) reported the estimate of 2,089,107 persons duplicated outside the surrounding blocks to the housing unit population and additionally 660,094 to group quarters (Table 1) (4). The sum, approximately 2.75 million, is plausibly lower than the estimate 3.73 million erroneous enumerations at an incorrect address. But the evidence from the success of computer matching within cluster compared to clerical suggests that the duplicates identified by computer matching are underestimates of total duplication. In fact, if the 37.8% efficiency observed by Mule were to apply to these estimates as well, then the total number of duplicates to group quarters and to housing units beyond the search area (hypothetically, 7.27 million) would be considerably larger than implied by the A.C.E. estimates of persons enumerated at an incorrect address, 3.73 million.

An analysis of Mule's results presented here suggests an alternative measure of efficiency. Before the A.C.E. eligible population in the census was defined, the Housing Unit Duplicate Operations removed from the A.C.E. universe approximately 6.0 million enumerated persons, largely through computer matching. When the success of computer matching is measured not only against the A.C.E. population but also the housing units reinstated or deleted during the Housing Unit Duplicate Operations, then computer matching found a proportion of duplicates higher than 37.8%. An analysis presented here suggests that the efficiency of computer matching within cluster was possibly as high as 75.7%. But this estimate is probably an upper bound on the efficiency for identifying duplicates beyond the search area or to group quarters. Thus, estimated duplicates with the assumption of 75.7% efficiency (Table 1) are likely to be underestimates.

Feldpausch (2001a) compared the duplicates identified by computer matching outside the search area to their classification in A.C.E. She noted that the erroneous enumeration rates were considerably lower than expected for these cases, but her report did not summarize the findings in terms of their implications for the A.C.E. estimate of erroneous enumerations. Her text suggests an estimate of 298,890 due to duplication to group quarters beyond the search area (Table 1). Approximate calculations in Section 4 indicate that the A.C.E. missed an estimated

498,070 erroneous enumerations from duplication with group quarters, including to group quarters within the search area, and 1,555,090 erroneous enumerations to the household population, for a total of 2,053,160 (Table 1).

As noted previously, the MER estimate 1,454,915 is itself the net of two estimates: 1,816,315 A.C.E. correct enumerations reclassified as erroneous and 361,400 A.C.E. erroneous reclassified as correct. Because the MER estimate of 1,816,315 A.C.E. correct enumerations should have included both situations where persons were duplicated and other situations not involving duplication, the estimate of 2,053,160 A.C.E. correct reclassified as erroneous for reasons of duplication based on Feldpausch (2001) logically should have been only part of the MER estimate of 1,816,315 A.C.E. correct reclassified as erroneous. In the extreme case that MER had caught none of these erroneous enumerations due to duplicates, adding the estimate of 2,053,160 from her study, plus 1,454,915 from the MER, would exceed the estimated undercount from the A.C.E. Allowance for 75.7% computer matching efficiency (Table 1) would increase the hypothetical sum further. The sum fails to account for the overlap between the studies, however (Fig. 1).

To assess the overlap, computer files from the duplication study and the MER (EFU review sample) were merged. The result confirmed that the MER found some of the duplicates missed by the A.C.E., but it failed to detect others. Using the estimation procedure implicit in the current estimate of 1,454,915 from the MER, an additional 1,125,377 should be added, to bring the total from the two studies to 2,580,292. The estimated 1,125,377 additional erroneous is the sum of 146,346 from group quarters and 979,031 others (Table 1).

But estimated increase, 1,125,377, does not reflect the efficiency of computer matching at finding duplicates. If the estimate of 75.7% based on the within cluster efficiency in the duplication study is used, then the estimate of the additional component, 1,486,257 (Fig. 1), raises the estimate of erroneous enumerations missed by the A.C.E. to 2,941,172 (Table 1). This estimated total is composed of an estimated 794,104 erroneous because of residence in group quarters and 2,147,067 others (Table 1).

The effect of underestimated erroneous enumerations leads the A.C.E. dual system estimate to overstate the true population. Although the A.C.E. used a poststratified dual system estimator with 416 cells, a single-cell approximation to the estimator implies that 2,941,172 missed erroneous enumerations would lead to an overstatement of the population by approximately 3.2 million.

2. THE MEASUREMENT ERROR REINTERVIEW (MER)

2.1 The A.C.E. E Sample

The basic sampling unit for the A.C.E. was the *cluster*, a grouping of one or more census blocks. Two overlapping samples were based on the same sample of clusters: a P sample that independently listed housing units in the cluster and interviewed residents in order to measure census omissions; and an E sample that checked whether a sample of census enumerations were correctly enumerated in the census. The sampling universe for the P sample, also termed the *A.C.E. universe*, was the household population of the U.S. except for remote areas in Alaska. Most, but not all, census household enumerations were eligible for E sample. Generally, only E-sample eligible persons were considered in determining whether a P-sample person matched to the census (5).

The E-sample component of the A.C.E., a sample of census enumerations, was used to estimate erroneous enumerations. Erroneous enumerations can be broadly categorized into *duplicates*, *fictitious enumerations*, *geocoding errors*, *other residence*, and *persons with insufficient information for matching*. *Duplicates*, that is, duplicates within the sample clusters or surrounding blocks, were identified clerically, as were *persons with insufficient information for matching*. Determination of *geocoding errors* required interviewers to find the census units but not necessarily to contact the residents. Identification of *fictitious enumerations* and *persons with other residence* on Census Day required collection of information from respondents who were frequently, but not always, members of the original census household.

In both the 1990 Post Enumeration Survey and the 2000 A.C.E., there was a residual category of E-sample *unresolved* cases. In both studies, a probability of correct enumeration was imputed for *unresolved* cases. In both, the imputed probability of erroneous enumeration ($= 1 - \text{probability of correct enumeration}$) was not categorized by type of erroneous enumeration. In 1990, the overall rate of erroneous enumeration was 5.74%, including an imputed contribution of 0.26% from *unresolved* (Feldpausch 2001b, p. 20). In 2000, the A.C.E. estimated a rate of 4.72%, including a contribution of 0.62% for *unresolved*. Much of the larger contribution in 2000 from *unresolved* can be attributed to stricter rules in 2000 for *other residence* Feldpausch (2001b, pp. 18-19). The contribution of *other residence* was 2.18% and 1.03%, in 1990 and 2000, respectively.

Feldpausch (2001b, pp. 20-21) redistributed the estimated probabilities of erroneous enumerations for *unresolved* in 1990 and 2000 into their likely categories, increasing the contribution of *other residence* to 2.29% and 1.41% in 1990 and 2000, respectively (Table 2). The redistribution lessens the gap between 1990 and 2000, but the difference between 1990 and 2000 in the estimates is about .88 percentage points. According to this redistribution of the *unresolved*, the 2000 A.C.E. appears to have estimated approximately 3.7 million erroneous

enumerations from *other residence*, approximately 2.3 million fewer than it would have at the rate estimated by the 1990 PES.

Besides the decline in *other residence*, there are other components with large changes. The changes in these components have been evaluated by other studies (6).

The A.C.E. E-sample interviewing occurred in two waves. A first wave corresponded to the initial interviewing for the P sample, accomplished by telephone (April 24 through June 13, 2000, 29.4% of total workload) and personal visit (June 18 through Sep. 1, except for one FL office completed by Sep. 11) (Hogan 2001, p. 25; Byrne et al. 2001, pp. 3, 7), using the same computer-assisted instrument. The initial interview determined both the current and Census Day residents. When P-sample Census Day persons were matched to the census and classified as residents, the corresponding census enumerations were classified as matched in the E sample and classified as correct census enumerations. The remaining census enumerations selected in the E sample were sent in the second wave during Oct. and Nov. 2000 to A.C.E. Person Followup (PFU). Some matched cases were also included in the second wave when the information was incomplete from the first wave. The PFU used a paper questionnaire. For the nonmatched E-sample cases, the PFU attempted to determine if the census enumerations represented valid Census Day residents.

Table 2 Comparison of percent erroneous enumerations by type from the 1990 PES and the 2000 A.C.E. after re-classifying the unresolved people. The PES rates pertain to a universe that includes noninstitutional group quarters, unlike the A.C.E. universe.

	1990 PES	2000 A.C.E.
Duplicate	1.66%	0.76%
Fictitious	0.22	0.50
Geocoding Error	0.38	0.25
Other Residence	2.29	1.41
Insufficient Information	1.19	1.80
Total	5.74%	4.72%

Source: Feldpausch (2001b, p. 21).

2.2 The Measurement Error Reinterview (MER)

The Measurement Error Reinterview (MER) was designed to evaluate both the P- and E-sample data collection. A sample of approximately 1/5 of the A.C.E. clusters was selected, followed by subsampling of housing units within the clusters sampled for the MER. With respect to the E sample, the MER's principle objectives were to detect errors in the A.C.E. measurement of

fictitious enumerations, geocoding errors, and other residence. The MER sample was reinterviewed with a paper questionnaire during Evaluation Followup (EFU) in Jan. and Feb. 2001.

Initial clerical coding of the MER/EFU results, later termed *EFU 1*, was partially supplemented with review by senior analysts. Interviewer notes were frequently consulted to classify cases. If the EFU results were incomplete or questionable, coders could reject the EFU results and substitute the A.C.E. results. On a weighted basis, approximately 6.4% of the EFU results were rejected (Adams and Krejsa, 2001, p. 12). The initial analysis of the EFU 1 estimated an A.C.E. understatement of erroneous enumerations of 1,919,029.

In response to a request from the Evaluation Steering Committee for A.C.E. Policy (ESCAP), Martin (2001) reviewed the paper questionnaires used for PFU and EFU. Her report detailed limitations with both questionnaires. The EFU questionnaire failed to ask the Census Day address for a number of situations in which the information would be required to make an unambiguous determination of erroneous enumeration (7). This logical flaw could have reflected the lack of field-testing of the EFU questionnaire prior to its use, unlike the PFU questionnaire, which was field-tested (Martin 2001, p. 2). In several other respects, however, the EFU questionnaire was superior in design to the PFU for clarifying concepts, and for reminding respondents by probing for details. Martin (2001, p. 8) judged both questionnaires as substantial improvements over the PES and evaluation questionnaires in 1990. On the other hand, she remarked that the extensive reliance on interviewer notes to code both the PFU and EFU questionnaires meant that the questions failed to reflect many persons' circumstances in a structured way (8). Both questionnaires were challenged by the complexity of census residency rules (Martin 2001, pp. 8-9). Martin did not review the Computer Assisted Personal Interview (CAPI) instrument used in the initial A.C.E. interview, however. Many, possibly the majority, of erroneous enumerations undetected by the A.C.E. were interviewed only with the CAPI instrument.

Because the EFU 1 analysis implied serious error in the A.C.E. but may itself have been subject to error including the logical flaw in the MER questionnaire, a subsample of the EFU sample, the Person Followup/Evaluation Followup Review (Adams and Krejsa 2001), was selected for systematic recoding by analysts, who were the staff most highly experienced in the coding phase of coverage studies. New coding procedures were established. The original A.C.E. codes (9), now identified as *PFU 1*, were reviewed and revised as appropriate using only the A.C.E. responses, to yield *PFU 2*. Similarly the EFU responses were recoded as *EFU 2*, using only EFU responses. Coders then combined the information into a *Best Code*. One of the guiding principles was to favor information from nonproxy respondents, who were members of the original E-sample household, over information from proxy respondents, who were not. Some types of proxy respondents were regarded as more informed than others. Other rules also attempted to follow the principle of using the information that appeared the most complete (Adams and Krejsa, 2001, p. 3). A *Conflicting* category was allowed for cases with contradictory geographic information or contradictory information on Census Day residence and the same type of respondent; that is, either both non-proxies or both proxies considered equally

informed. The EFU 2 coding recognized the logical flaw in the EFU questionnaire, coding cases with another Census Day address that was not recorded to unresolved instead of erroneous as in EFU 1 (Adams and Krejsa 2001, pp. 2, 3, 13). To analyze the results, Adams and Krejsa compared the PFU 1 code to the Best Code (Table 3).

Table 3 Comparison of A.C.E. (PFU 1) to Best Code from the PFU/EFU Review. For PFU 1, total correct enumerations are divided into those matched to P-sample residents and nonmatched correct enumerations in the census. Estimates are weighted by MER review weights, reflecting A.C.E. sampling, MER subsampling, and subsampling for the review sample.

PFU 1 Code	Best Code from Second Review				
	Correct	Erroneous	Unresolved	Conflicting	Total
Total Correct Enumerations	238,786,314	1,816,315	9,151,011	1,613,442	251,367,081
<i>Matched</i>	<i>210,222,189</i>	<i>1,139,407</i>	<i>8,763,973</i>	<i>563,514</i>	<i>220,689,083</i>
<i>Nonmatched Correct Enum.</i>	<i>28,564,125</i>	<i>676,908</i>	<i>387,038</i>	<i>1,049,928</i>	<i>30,677,998</i>
Erroneous	361,400	2,936,887	186,418	666,512	4,151,217
Unresolved	2,529,422	664,929	3,303,074	314,685	6,812,110
Total	241,677,134	5,418,131	12,640,503	2,594,639	262,330,408

Source: Adams and Krejsa (2001, p. 7).

Based on Table 3, Adams and Krejsa reported an estimate of the net understatement of erroneous enumerations by the A.C.E. of 1,454,915. To represent their estimator, let M_{ij} denote the estimated frequencies in Table 3, where i denotes PFU 1 outcomes C , E , U or “.” for total correct enumerations (both matched and nonmatched correct enumerations), erroneous, unresolved, and total, respectively, and j denotes Best Codes C , E , U , Cf , or “.” for correct, erroneous, unresolved, conflicting, and total. The estimate of 1,454,915 is the difference of two cells in Table 3: $M_{C,E} = 1,816,315$ A.C.E. correct enumerations reclassified as erroneous, and $M_{E,C} = 361,400$ A.C.E. erroneous reclassified as correct. Their estimator is

$$B_{MER} = M_{C,E} - M_{E,C} \quad (1)$$

Estimating the net error in A.C.E. according to eq. (1) implicitly uses the remaining information in Table 3 in the following manner:

- $M_{C,U} = 9,151,011$ and $M_{C,Cf} = 1,613,442$ correct enumerations in PFU 1 classified as unresolved or conflicting, respectively, by the Best Code are effectively treated as correct, because this information is not reflected in eq. (1);

- $M_{E,U} = 186,418$ and $M_{E,Cf} = 666,512$ erroneous enumerations in PFU 1 classified as unresolved or conflicting, respectively, by the Best Code are effectively treated as erroneous, because this information is also not reflected in eq. (1); and
- A.C.E. imputations for $M_{U,.} = 6,812,110$ are accepted without modification by the information from the Best Code.

In short, the estimated net error is based on the only two cells, $M_{C,E}$ and $M_{E,C}$, in which a Best Code of erroneous or correct revises an A.C.E. one with the opposite value.

Of the $M_{C,E} = 1,816,315$ A.C.E. correct enumerations reclassified as erroneous, an estimated 614,451, approximately 1/3, were because the person should have been counted in group quarters, including 315,406 in dorms (Adams and Krejsa 2001, p. 9). An additional 976,343 were attributed to other residence issues, 28,729 to *fictitious*, 120,530 to *geocoding*, and 76,262 for other reasons (10). The estimate for other residence issues includes 73,940 for *joint custody*.

Of the $M_{E,C} = 361,400$ A.C.E. erroneous enumerations reclassified as correct, an estimated 13,622 were classified as living in group quarters by A.C.E. but changed to valid residents in the review (Adams and Krejsa, p. 10). Thus, the estimated net error due to residence in group quarters is 600,829 ($=614,451 - 13,622$) (Table 1).

Adams and Krejsa (2001, p. 15) remark on the sensitivity of their findings to alternative assumptions about the unresolved and conflicting cases. Overall, an estimated 9,337,429 cases coded as correct or erroneous in PFU 1 became unresolved ($M_{C,U} + M_{E,U}$). Unlike EFU 1, unresolved cases in EFU 2 include cases with another Census Day address that was not recorded because of the logical error in the EFU form, and these in turn contributed to unresolved for Best Code. These cases are largely analogous to the group of cases in the A.C.E. E sample requiring imputation of the probability of correct enumeration: those with another Census Day residence, where the address had not been recorded (Feldpausch 2001b, pp. 18-19, cited previously; also Cantwell and Childers 2001). In A.C.E., the unresolved in this category were imputed an estimated average probability of correct enumeration of approximately 0.23, much lower than most other categories (Cantwell et al. 2001, p. 42). Applying a similar approach to unresolved EFU 2/Best Code outcomes would increase the estimated erroneous enumerations, compared to the assumptions implicit in eq. (1).

An estimated 2,279,954 cases coded as correct or erroneous in PFU 1 became conflicting ($M_{C,Cf} + M_{E,Cf}$). Conspicuously, these are disproportionately drawn from PFU 1 nonmatched correct enumerations and erroneous enumerations.

3. THE PERSON DUPLICATION STUDY

As noted previously, the A.C.E. estimate of duplicates within block is quite accurate (Bean 2001, p. 22). The A.C.E. estimate of duplicates shown in Table 2 also includes a smaller number of duplicates to surrounding blocks in the search area.

Beyond search area, however, the A.C.E. measured duplicate enumerations indirectly, as part of two other categories of erroneous enumerations. The same strategy was used by the 1990 PES. The first category is *geocoding error*: If the census incorrectly assigns an address to a block outside of the search area, then the case is classified as a *geocoding error*. The census sometimes duplicates a unit by including it in both an incorrect block and the correct one. In the A.C.E. estimation, a duplicated unit is counted as an erroneous enumeration due to *geocoding error* when the enumeration in the wrong block is selected in the E sample, and as a correct enumeration when the correct block is selected. The second category is *other residence*: If a duplicate occurs between a correct enumeration and an incorrect one at the wrong residence, the person is counted as correct when the correct address is selected, and as erroneous when the wrong residence is selected. As previously recognized (11), estimates of *other residence* include both duplicate enumerations of persons enumerated correctly at their Census Day address, and persons who are only counted at the wrong address.

A person duplication study was initiated in 2001 in part to investigate issues arising from the Housing Unit Duplication Operations (Nash 2000, Fay 2001), which were part of census operations in 2000. The Housing Unit Duplication Operations attempted to correct problems in the development of the Master Address File (MAF) for the census—the MAF duplicated some housing units, often with similar but not identical address descriptions. The duplication of housing caused the duplicate enumeration of persons in early census returns. As an example, when the MAF had included separately “Apt 1A” and “Unit A1” at the same street address, the early census returns had often counted the same households at both.

The Housing Unit Duplication Operations were divided into two phases for purposes of timing, particularly with respect to the A.C.E. (12). In the first phase, addresses were linked either by rules applied to the address entries in the MAF or by computer matches of housing units apparently containing the same people. Person matching was carried out in two steps: a first step of finding exact matches of persons with the identical first and last names, and month, day, and year of birth, and a second step of evaluating the similarities of households linked by one or more exactly matching people. Person matching was restricted to households in the same state and within 30 miles of each other. For each pair of units linked either by address edits or person matching, one unit was selected to remain in the census, and the other was removed from the A.C.E. universe (13).

In the second phase of the Housing Unit Duplication Operations, more detailed criteria were developed and applied to determine which of the units removed from the A.C.E. universe in the first phase would be reinstated into the census. Phase 2 reinstated 2,315,553 persons and

1,002,951 housing units into the census, and deleted the remaining 3,572,799 persons and 1,371,320 housing units from the census. The reinstated units were included in the census count but excluded from the A.C.E. universe. Although the number of reinstated persons is large, Raglin (2001) showed that the effect on the A.C.E. dual system estimate of total population was minor.

In spring 2001, a team of Census Bureau staff began a study of computer matching of the A.C.E. sample to the entire census nationally (Mule 2001). The study had multiple objectives, including to account for the drop in estimated *duplicates* from 1990 to 2000 (Table 2) and to investigate the quality of reporting of *other residence* in the A.C.E. A source file comprising the A.C.E. E-sample eligible units and reinstated units in the A.C.E. sample clusters was matched to a target file comprising the enumerated persons in census housing units (except for reinstated units), group quarters, reinstated units, and deleted units (even though deleted units are excluded from the final census).

Computer matching methods were similar to those used during the Housing Unit Duplication Operations, but they incorporated several refinements. The first stage was again based on exact matching, but this time the matching also considered middle initials. Some errors in the capture of names were repaired prior to the match (14), and some combinations of names and birthdays identified and removed from analysis, including the tendency, particularly among the Hispanic population, to name a child born on an important Saint's Day after the saint (15).

The second stage of matching considered households linked together by one or more exact matches. Possible matches between the remaining persons were evaluated with Census Bureau matching software based on the Fellegi-Sunter (1969) algorithm. Some of the exact matches from the first stage were evaluated for coincidental sharing of birthday. Because some combinations of first and last names are common, such as "Linda Smith," a model weight was developed to adjust for the probability of two persons with the same name sharing a birthday (Mule 2001, pp. J-3 to J-4). Model weights of 1 or 0 were assigned for the remaining cases according to Table 4.

The team developed rules to reduce the chance of false matches by dropping a number of preliminary matches from the analysis. More evidence was required for matches between different states than within (Table 4). The rules permitted single individuals to match, including to group quarters, through first-stage matches only.

The estimates used matches from both the first and second phases. The duplicates were weighted by the product of A.C.E. sampling weights, the model weights for coincidental birth, and multiplicity weights (Sirken 1972).

Table 4 Duplicate study rules for retaining matches based on the number of persons linked between households, stage, and geography. The category with weight 0 was dropped from the analysis.

Category	Stage	Model Weight
Same State		
2+ links, 1-1 match of households	1st or 2nd	1
2+ links, not all persons matched	1st or 2nd	1
1 link only (including to group quarters)	1st	model
Different State		
2+ links, 1-1 match of households	1st or 2nd	1
2+ links, not all persons matched	1st	model
2+ links, not all persons matched	2nd	0
1 link only (including to group quarters)	1st	model

Source: Table J2, p. J-2, Mule (2001). A category involving only 6 cases with links within the same housing unit is omitted here.

The multiplicity weights were a key feature of the estimation. The E sample was a sample of census enumerations, not a sample of persons, so each enumeration of the same person had its own chance of selection. For example, when an enumerated A.C.E. household duplicated another enumeration of the household not in a different cluster, a multiplicity weight of 1/2 was applied because either enumeration was eligible for selection into the A.C.E. (Mule 2001, p. 6 and App. G). Multiplicity weights were not required in some other instances, such as duplication to group quarters, because group quarters were not sampled for the A.C.E.

Table 5 summarizes the resulting estimates. The large number of duplicates identified between the A.C.E. E sample and reinstated and deleted units reflects the basic design of the Housing Unit Duplication Operations, which used computer matching to identify possible duplicates. Mule (2001, pp. 9-10) showed that if duplicates to reinstates and group quarters within the search area were added to the A.C.E. estimate of duplicates to the E-sample eligible universe, then the outcome would have been considerably closer to 1990 levels of duplication and that, if duplicates to deleted units were also added, the result would have exceeded 1990 levels.

Table 5 Estimated number of computer matches from the 2001 computer match study of census person duplicates. Reinstated and deleted units were determined by the Housing Unit Duplication Operations; neither are included in the A.C.E. universe, and deleted units are not included in the final census. Estimates are weighted by A.C.E. sampling weights, multiplicity weights, and weights computed from the Poisson model for coincidental birth.

	Within Cluster	Surrounding Blocks	Beyond Search Area	Total
E-sample Elig. to E-sample Elig.	724,687	146,880	2,089,107	2,960,675
E-sample Elig. to Reinstated	1,049,699	24,029	573,699 ^a	1,647,426 ^a
E-sample Elig. to Deleted	1,941,732	682,909	276,968 ^b	2,901,609 ^b
E-sample Elig. to Group Quarters	103,168	46,736	510,190 ^c	660,094 ^c

Source: Mule (2001) Table 2 (p. 9) and Table 6 (p. 11). Cells are noted where the estimate shown may contain small numbers of matches of reinstated to reinstated, deleted, and group quarters beyond the search area.

Notes: a. Includes a presumably small number of duplicates of reinstated to reinstated beyond the search area.

b. Includes a presumably small number of duplicates of reinstated to deleted beyond the search area.

c. Includes a presumably small number of duplicates of reinstated to group quarters beyond the search area.

Because computer matching did not detect all duplicates in the census, it is helpful to have some measure of the efficiency of computer matching in order to interpret the results. Mule compared A.C.E. clerical performance with computer matching within the search area (Table 6) and reported (2001, p. 9) that computer matching within cluster found only 37.8% the number of duplicates as the A.C.E. But if all enumerated census housing units are considered—that is, before the Housing Unit Duplication Operations had deleted some units and removed the reinstated units from the A.C.E. universe—computer matching would have matched an estimated 3.7 million persons ($=724,687+1,049,699+1,941,732$) within cluster. Assuming also that clerical matching would have found no additional matches to the reinstated or deleted units, then computer matching may have been as much as 75.7% (16) efficient at finding duplicates within cluster. To the extent that clerical matching may have found some additional matches to the reinstated or deleted units, the efficiency would be somewhat lower.

In this analysis, the efficiency of computer matching is of interest for two groups where the efficiency relative to clerical matching was not observed: (1) matches to the group quarter universe, both within and beyond the search area; and (2) matches to the E-sample eligible population beyond the search area. As noted in Table 4, the only matches allowed to group quarters were those from phase 1, and all such matches were evaluated under the Poisson model. The Housing Unit Duplication Operations did not affect group quarter enumerations and, in that respect, the efficiency of computer matching should be more analogous to the efficiency of

computer matching to all census enumerations than to the universe left after reinstated and deleted units were excluded from the A.C.E. universe. Similarly, the majority of matches beyond the search area would not have been affected by the Housing Unit Duplication Operations because of their use of a 30-mile limit on identifying matches. (Matching households within the 30-mile limit would have been affected, which would have the effect of reducing the efficiency of computer matching within the 30-mile limit because the Housing Unit Duplication Operations had removed one from each pair of matches identified in its computer matching.)

Table 6 Comparison of A.C.E. and computer match study of census duplicates within the A.C.E. search area. Estimates are weighted by A.C.E. sampling weights, multiplicity weights, and weights computed from the Poisson model for coincidental birth.

	Within Cluster	Surrounding Blocks	Total Within Search Area
A.C.E. clerical estimate	1,916,340 ^a	98,335 ^a	2,014,675
Computer: E-sample Elig. to E-sample Elig.	724,687	146,880	871,567
Computer: E-sample Elig. to Reinstated	1,049,699	24,029	1,073,728
Computer: E-sample Elig. to Deleted	1,941,732	682,909	2,624,641
Total Computer	3,716,118	853,818	4,569,936
Computer: E-sample Eligible to Group Quarters	103,168	46,736	149,904

Source: Mule (2001) Table 2 (p. 9), except where noted.

Note: a. Computed by Thomas Mule but not shown separately in his report.

There are a number of reasons that the 75.7% efficiency would overstate the efficiency of computer matching outside of the search area or to group quarters:

- As previously noted, the estimation of 75.7% ignores possible additional clerical matches to the reinstated or deleted households;
- The rules in Table 4 favor the matching of whole households, generally the situation addressed by the Housing Unit Duplication Operations, but they are more cautious in retaining partial households or single individuals as confirmed matches;
- Matches to different states require more evidence than within state; and
- Matches to group quarters or to single persons within households only succeed if matched at the first stage.

Thus, the estimate of 75.7% is interpreted in subsequent calculations as if it were an upper bound on the efficiency of computer matching.

In summary, computer matching detected about 2.7 million duplicates to group quarters or to the E-sample population beyond the search area (Table 1). An allowance for 75.7% computer efficiency at detecting duplicates raises the total to 3.6 million (Table 1). These estimates, by themselves, do not measure errors in the A.C.E. directly, because the A.C.E. E sample arguably may have treated all of them as erroneous enumerations.

4. COMPARING CENSUS DUPLICATION TO THE CORRESPONDING A.C.E. ENUMERATION STATUS

4.1 Primary Re-Analysis

Feldpausch (2001a) analyzed the A.C.E. Enumeration Status from the duplication study. Because Mule (2001) had primarily analyzed the results within the search area, Feldpausch concentrated on matches beyond the search area. She tabulated duplicates of A.C.E. sample cases from the person duplication study to the E-sample eligible universe and group quarters. She distinguished between group quarters where persons could claim that they had a usual home elsewhere (UHE), such as military barracks and soup kitchens, from others, such as college dormitories, nursing homes, and jails, where census rules required that the residents be counted at their group quarters. To restrict the analysis to likely duplicates, she included only cases with model weight > 0.5 based on the Poisson model (Table 7). Her report does not account for her decision to exclude the weight from the Poisson model in weighting the estimates.

Feldpausch (2001a, p. iii) concluded “There is evidence that the A.C.E. did not code as erroneous enumerations some people who should have been coded erroneous due to other residences.” Her report did not provide a quantitative estimate of the effect of this error on the A.C.E. estimate of erroneous enumerations, however (17).

An approximate estimate of how much the A.C.E. understates erroneous enumerations, most of which should have been *other residence*, can be based on the results in Table 7. The estimates for the E-sample eligible population include multiplicity weights, generally $1/2$, to compensate for the essentially doubled chance of selection because the duplicate can be identified when either enumeration of the pair falls into the E sample. Consequently, the estimated 2,169,366 duplicates in Table 7 represents a number of erroneous enumerations that the A.C.E. should have captured. The table shows only 307,138 estimated A.C.E. erroneous enumerations, but this estimate also includes multiplicity weights of generally $1/2$. Thus, 307,138 should be multiplied by approximately 2 to compensate for the effect of multiplicity weighting, in order to approximate the contribution of these cases to the estimated erroneous enumerations in the A.C.E. (In fact, the factor should be slightly greater than 2 for a different reason, to compensate for the model weights reflected in the table. In fact, however, most of these weights were close to 1.) Consequently, the results imply approximately $2,169,366 - 2(307,138) = 1,555,090$ undetected erroneous enumerations from duplication to the household universe.

Table 7 Estimated E-sample duplicates to enumerations outside the search area. Estimates for group quarters are distinguished by whether a usual home elsewhere (UHE) could be reported. Estimates are weighted by A.C.E. sampling weights and multiplicity weights, but omit the weight based on the Poisson model. Only duplicates with weight > 0.5 from Poisson model are included. Imputed probabilities of correct enumeration are used to apportion cases where the enumeration status was unresolved.

Final Match Code	Housing Units	Group Quarters			
	E-Sample Eligible HU	Cannot Claim UHE		Can Claim UHE	GQ Total
		Dorm	Other		
Total Correct Enumerations	1,862,228	147,901	158,436	52,139	358,477
<i>Matched</i>	<i>1,298,084</i>	<i>93,846</i>	<i>103,871</i>	<i>40,378</i>	<i>238,095</i>
<i>Nonmatched Correct Enum</i>	<i>564,144</i>	<i>54,055</i>	<i>54,565</i>	<i>11,761</i>	<i>120,382</i>
Erroneous	307,138	123,257	31,320	7,447	162,024
Total	2,169,366	271,158	189,756	59,586	520,501

Source: Feldpausch (2001a) Table 1, p. 4, and Table 3, p. 6.

Duplicates to group quarters where persons cannot claim UHE are generally evidence of erroneous enumerations, because in these group quarters census rules require the persons to be counted there (18). Thus, 306,337 (=271,158 + 189,756 - 123,257 - 31,320) represents an approximate estimate of undetected erroneous enumerations from duplication to group quarters where UHE is not allowed.

The issue of duplicates to the group quarters where persons can claim UHE is open to different interpretations. Feldpausch (2001a, p. 4) interprets this group as correct enumerations in the A.C.E. universe, and assumes that duplicates represent erroneous enumerations in the group quarters universe. Under this interpretation, the estimated 7,447 erroneous enumerations for this group are correct enumerations in the E-sample population, and the remaining 52,139 estimated correct enumerations are also correct for the E-sample eligible population. This interpretation implicitly assigns 59,586 erroneous enumerations to the count for group quarters.

But residence rules for the Census 2000 are more complex (19), and the status of *can claim UHE* is not equivalent to *must claim UHE*. A second possible interpretation is to take the A.C.E. entirely at face value. Thus, the 7,447 could be interpreted as erroneous enumerations in the E-sample eligible population successfully identified by the A.C.E., such as when a member of the armed forces lives and sleeps the majority of time in barracks but is also erroneously counted as

a member of an off-base household. Possibly, the remaining 52,139 duplicates are correct enumerations in the E-sample eligible population, but erroneous enumerations in the count for group quarters.

If the E-sample interview often failed to detect other residences, however, as evidenced from the results presented in Table 7 for other types of group quarters, then many of the duplicates to group quarters where UHE is allowed may represent erroneous enumerations in the E-sample eligible population. This interpretation allows up to an additional 52,139 undetected erroneous enumerations.

Although Feldpausch limits her analysis to duplicates outside of the search area, all duplicates to group quarters are of interest, including those within the search area. The number of duplicates undetected by the A.C.E. can be approximately estimated as the difference, 498,070, of the total number of duplicate enumerations to group quarters, 660,094 (Table 5), and the estimated number of erroneous enumerations in Table 7, 162,024. Unlike duplication to the housing unit population, the issue of multiplicity weighting does not arise because group quarters were excluded from the A.C.E. universe. This approximation overlooks the possibility that some A.C.E. duplicates to group quarters within the search area may have been classified as erroneous for other reasons. The analysis in the next section avoids this assumption.

In summary, re-analysis of Feldpausch (2001) suggests the estimate of 2,711,556 erroneous enumerations missed by the A.C.E. (Table 1). This estimate may be split into 657,788 for group quarters and 2,053,767 other, if an estimated efficiency of 75.7% is used (Table 1). Because these estimates may overlap with the findings of the EFU review, the results from the two studies cannot be simply added.

4.2 Further Analysis of Group Quarters with UHE Allowed

Census 2000 counted 7,778,633 in group quarters: 4,059,039 in the institutional population and 3,719,594 in the noninstitutional. The issue of how to interpret duplicates to group quarters where UHE is allowed touches on the larger context of the Census Bureau's decision to design the A.C.E. to correct the census count by only correcting the census count in the A.C.E. universe and specifically to omit group quarters from that universe (Killion 1997). In general, the strategy may be represented as the following:

$$\begin{aligned} \text{Corrected U.S. Population} = & \text{Corrected population in A.C.E. universe} + \\ & \text{census count outside the A.C.E. universe} . \end{aligned} \tag{2}$$

The strategy implicitly relies on an assumption that the net error of the second term is small. Originally, the primary basis for omitting group quarters from the A.C.E. universe was the past experience indicating that dual-system estimation could not succeed for group quarters (Killion 1997). Instead, enhanced census methods were proposed to produce an accurate count for the group quarters population. Thus, the original decision was argued from necessity and defined an

objective for the quality of the group quarters count. Subsequent general descriptions (20) of the A.C.E. have generally not emphasized or clarified the assumptions underlying eq. (2).

An internal review of the group quarters count in Census 2000 (Smith 2002) assesses the consistency of the group quarters count relative to independent estimates. The independent estimates were constructed in various ways, such as a completely independent source (correctional facilities, nursing homes); an independent estimate of a change or rate of change since the 1990 census, which was combined with the 1990 census count (college dormitories, group homes); population rates from the 1990 census applied to the 2000 census (juvenile institutions) or independent estimates (military quarters); or simply the proportional growth in total population from 1990 to 2000 to project the component of the group quarters population (all others). In this review, the group quarters where UHE is allowed includes military quarters (355,155), total staff (17,366), group homes (454,055), and “other noninstitutional” (828,890), which combines UHE allowed with some categories of UHE not allowed (Smith 2002, Table 1). Where independent estimates are available for some of these groups, the independent estimates are based on the 1990 census.

Consequently, because there is scant evidence on the quality of the census count for group quarters where UHE is allowed, the implications of duplicates between these group quarters and the A.C.E. universe remains unclear. Although eq. (2) appears to require only that there be a small net error in the count for the census count outside the A.C.E. universe, an accurate count of the group quarters—in the sense that the census count all group quarters persons and only those persons who belong there—appears necessary in order to avoid complex assumptions about how persons incorrectly counted there may be counted in the A.C.E. universe. Feldpausch lists as an assumption (2001a, pp. 2-3) “there was a high quality group quarters enumeration. If this is not the case, the results regarding E-sample people duplicated to group quarters need to be reexamined.” The precise meaning of this remark is unclear, particularly with respect to the distinction between UHE allowed and UHE not allowed.

The analysis in this section and the next includes duplicates to group quarters where UHE is permitted as erroneous enumerations, even though alternative interpretations are possible. Fortunately, the estimated number of cases at issue, 59,586, is small relative to the overall analysis.

5. THE MERGED MER AND PERSON DUPLICATION STUDIES

To interpret the joint implications of the MER review and person duplication studies, their files were merged (21). The merged file was restricted to the EFU review sample, and EFU review weights were used in the analysis. For simplicity, only duplicates with model weights greater than .98 under the Poisson model for coincidental births were included (22).

5.1 Analysis of Group Quarters Population

Table 8 mirrors Table 3 but displays EFU review sample cases identified as duplicates to group quarters.

Table 8 Comparison of A.C.E. (PFU 1) to Best Code from the PFU/EFU review for persons matched to the group quarters universe in the person duplication study, with model weight from the Poisson model $> .98$. Estimates are weighted with EFU review weights. (Standard errors in parentheses, using a simple jackknife of sample clusters in the EFU.)

PFU 1 Code	Best Code from Second Review				
	Correct	Erroneous	Unresolved	Conflicting	Total
Total Correct Enumerations	93,057 (51,255)	54,849 (18,571)	24,507 (24,507)	28,782 (10,918)	201,195 (60,668)
<i>Matched</i>	67,036 (45,012)	27,756 (14,272)	24,507 (24,507)	0 (0)	119,299 (53,159)
<i>Nonmatched Correct Enum</i>	26,022 (24,553)	27,093 (11,915)	0 (0)	28,782 (10,918)	81,896 (29,412)
Erroneous	0 (0)	118,812 (21,746)	491 (491)	8,647 (5,302)	127,950 (22,362)
Unresolved	5,901 (2,538)	2,648 (2,361)	7,608 (4,807)	1,965 (1,670)	18,122 (6,418)
Total	98,958 (51,312)	176,310 (28,564)	32,606 (27,541)	39,393 (12,237)	347,267 (66,021)

Restricting Table 8 to cases with model weight $> .98$ produces a lower estimated total, 347,267, than 520,501 in Table 7, although the difference is also due to the different samples in the two tables. Using the notation of Section 2, let $DG_{i,j}$ denote the estimated duplicates to group quarters in Table 8. Of $DG_{..} = 347,267$ duplicates in group quarters, $DG_{E..} = 127,950$ were identified by the A.C.E., $DG_{..E} = 176,310$ were identified by the Best Code, and $DG_{E,E} = 118,812$, were identified as erroneous by both. The MER estimate of bias, eq. (1), includes $DG_{C,E} = 54,849$. But the duplicate study provides evidence of additional underestimation of erroneous enumeration not captured by eq. (1), by estimating nonzero values in 3 of the following 4 cells:

- $DG_{C,C} = 93,057$ PFU 1 Correct to Best Correct
- $DG_{C,U} = 24,507$ PFU 1 Correct to Best Unresolved
- $DG_{C,Cf} = 28,782$ PFU 1 Correct to Best Conflicting
- $DG_{E,C} = 0$ PFU 1 Erroneous to Best Correct

The total is 146,346 (se=57,800) additional duplicates to group quarters, unmeasured by PFU 1 and the estimator given by eq. (1). Possibly, some of these cases may be duplicates to group quarters where UHE is allowed, with the attendant difficulties of interpretation discussed in the previous section. Formally, the estimator of additional bias from duplicates to the group quarters population may be written

$$ABG_{DUP} = DG_{C,C} + DG_{C,U} + DG_{C,Cf} + DG_{E,C} \quad (3)$$

This estimator, like eq. (1), does not alter the assumptions made about unresolved PFU 1 cases, namely, that the A.C.E. imputation procedures represent the correct proportion of erroneous enumerations among unresolved PFU 1 cases.

An allowance for 146,346 (Table 1) additional duplicates is considerably less than the estimated 614,451 E-sample correct enumerations reclassified as erroneous by the MER (the estimate on which the net estimate, 600,829, in Table 1 is based). This suggests that the MER may have succeeded at identifying the majority of erroneous enumerations missed by the A.C.E. when the persons were residents of group quarters.

5.2 Analysis of the E-sample Eligible Population

Similarly, Table 9 mirrors Table 3 for duplicates to the E-sample eligible population. Three factors account for differences between total duplicates in Table 7 and Table 9: (1) the use of the full A.C.E. sample in Table 7 and the MER/EFU review sample in Table 9; (2) more restrictive conditions on the model weight in Table 9; and (3) the use of multiplicity weights in Table 7, generally $\frac{1}{2}$ for matches to E-sample eligible housing units. The combination of the last two reasons accounts for why the estimated total in Table 9 is somewhat less than twice that in Table 7.

There are 3,895,044 total duplicates without considering multiplicity. Only about half of these, 1,947,522, should be correct enumerations. The following cells are considered to be correct enumerations in eq. (1), which estimates the bias in the A.C.E. on the basis of the EFU review:

- $DE_{C,C} = 2,667,580$ PFU 1 Correct to Best Correct
- $DE_{C,U} = 162,181$ PFU 1 Correct to Best Unresolved
- $DE_{C,Cf} = 94,244$ PFU 1 Correct to Best Conflicting
- $DE_{E,C} = 2,548$ PFU 1 Erroneous to Best Correct

Table 9 Comparison of A.C.E. (PFU 1) to Best Code from the PFU/EFU Review for persons matched to the E-sample eligible universe in the person duplication study, with model weight from the Poisson model > .98. Estimates are weighted with EFU review weights, but do not include a multiplicity weight. (Standard errors in parentheses)

PFU 1 Code	Best Code from Second Review				
	Correct	Erroneous	Unresolved	Conflicting	Total
Total Correct Enumerations	2,667,580 (360,840)	191,047 (62,203)	162,181 (85,224)	94,244 (37,230)	3,115,053 (381,704)
<i>Matched</i>	2,123,795 (338,621)	131,842 (55,653)	143,875 (84,804)	4,500 (4,500)	2,404,013 (357,980)
<i>Nonmatched Correct Enum.</i>	543,785 (116,860)	59,205 (27,661)	18,306 (8,607)	89,744 (36,962)	711,040 (127,165)
Erroneous	2,548 (1,679)	391,371 (55,550)	9,866 (5,344)	58,405 (18,732)	462,190 (60,273)
Unresolved	69,669 (14,770)	44,889 (11,992)	168,205 (31,490)	35,037 (14,039)	317,801 (39,796)
Total	2,739,797 (360,866)	627,307 (85,900)	340,252 (92,066)	187,687 (43,846)	3,895,044 (393,914)

The total of these four components is 2,926,553, all treated as correct if the EFU review and A.C.E. are combined. Because the total number of correct enumerations among these linked cases should only be 1,947,522, the total implies that the EFU review underestimates erroneous enumerations by 979,031 (= 2,926,553 - 1,947,522; se=188,473) from undetected duplicates within the A.C.E. universe. This estimate can then be combined with duplicates or other erroneous enumerations identified in MER. Formally, the estimator of additional bias from duplicates to the E-sample eligible population may be written

$$ABE_{DUP} = DE_{C,C} + DE_{C,U} + DE_{C,Cf} + DE_{E,C} - .5 DE_{..} \quad (4)$$

It may also be written

$$ABE_{DUP} = .5 DE_{..} - DE_{E,E} - DE_{E,U} - DE_{E,Cf} - DE_{C,E} - DE_{U,.} \quad (5)$$

As in eq. (3), the estimator assumes that the A.C.E. imputation procedures represent the necessary proportion of erroneous enumerations among the unresolved.

The estimate of additional erroneous enumerations, 979,031, implied by the duplicates is approximately the same size as the MER estimate of erroneous enumerations, 976,343, (Adams and Krejsa 2001, p. 9) due to other residence issues excluding group quarters, as described in Section 2. Thus, with respect to duplicates to the E-sample eligible population beyond the

search area, the information from the duplication study appears to approximately double the estimate available from the MER for other residence issues excluding group quarters.

5.3 Combined Analysis

To represent the possible effect of the efficiency of computer matching, each term of eq. (3) and (4) was assumed proportionately understated. As a logical constraint, the effect of adding the adjusted estimates from Tables 8 and 9 should not exceed the corresponding entries of Table 3, and this constraint is not violated for the assumed 75.7% efficiency. With an allowance for 75.7% efficiency, the estimated additional erroneous enumerations from duplication to group quarters increases from 146,346 to 193,275 and to the E-sample eligible universe from 979,031 to 1,292,981 (Table 1). Even with this adjustment, (1) the MER detected more erroneous enumerations due to other residence in group quarters than the duplicate analysis; and (2) the MER detected, within sampling error, roughly the same number of erroneous enumerations due to other residence in the E-sample eligible population beyond the search area as the duplicate analysis.

Table 10 summarizes the separate contributions of eq. (1) from the MER/EFU review sample and the sum of eq. (3) and (4) from the duplicate study. The table shows results separately for Non-Hispanic Blacks, for Hispanics, and for Non-Hispanic Whites and all other races, classified according to the A.C.E. poststratification.

Table 11 repeats the analysis for the age/sex classification used by A.C.E. poststratification. The additional effect of duplicates on 18-29 males or 18-29 females is less than the effect measured by the MER. The combined effect of MER plus the duplicates is particularly large for 18-29 females and small for 30-49 females, although these differences are principally due to the MER contribution rather than the addition from the duplicate study. Nearly 40% of the estimated total from additional duplicates is contributed by the 0-17 age group, suggesting that this group merits specific study. (The standard error of the estimate is large, however.)

Table 10 Estimates of erroneous enumerations missed by the A.C.E. according to the MER and person duplication study. A combined effect is estimated for duplicates without any adjustment for the efficiency of computer matching, and with a 75.7% adjustment applied uniformly. Estimates are based on the MER/EFU review subsample. Race and ethnicity categories are based on the A.C.E. poststratification. (Standard errors in parenthesis)

	NonHisp Blacks	Hispanics	All Others	Total
MER only	186,028 (58,056)	221,241 (79,329)	1,047,646 (165,010)	1,454,915 (193,124)
Addl dups, unadj	171,635 (56,172)	211,684 (81,982)	742,058 (170,858)	1,125,377 (199,334)
Total, unadj	357,663 (75,842)	432,925 (110,287)	1,789,704 (248,953)	2,580,292 (283,738)
Addl dups, adj	226,674 (74,184)	279,566 (108,271)	980,017 (225,648)	1,486,257 (263,255)
Total, adj	412,702 (88,612)	500,807 (129,969)	2,027,663 (292,376)	2,941,172 (333,454)
As percent of total E-sample population				
MER only	.63 (.19)	.71 (.25)	.52 (.08)	.55 (.07)
Addl dups, unadj	.58 (.19)	.68 (.25)	.37 (.08)	.43 (.08)
Total, unadj	1.20 (.25)	1.39 (.33)	.89 (.12)	.98 (.11)
Addl dups, adj	.76 (.25)	.89 (.33)	.49 (.11)	.57 (.10)
Total, adj	1.39 (.29)	1.60 (.39)	1.01 (.14)	1.12 (.12)

Table 11 Estimates of erroneous enumerations missed by the A.C.E. according to the MER and person duplication study. A combined effect is estimated for duplicates without any adjustment for the efficiency of computer matching, and with a 75.7% adjustment applied uniformly. Estimates are based on the MER/EFU review subsample. (Standard errors in parenthesis)

	Total	0-17	18-29 Male	18-29 Female
MER only	1,454,915 (193,124)	249,051 (67,616)	221,210 (62,569)	319,996 (79,552)
Addl dups, unadj	1,125,377 (199,334)	432,629 (107,583)	70,321 (37,663)	115,716 (56,039)
Total, unadj	2,580,292 (283,738)	681,680 (122,295)	291,531 (73,183)	435,712 (89,259)
Addl dups, adj	1,486,257 (263,255)	571,362 (142,082)	92,871 (49,741)	152,823 (74,009)
Total, adj	2,941,172 (333,454)	820,413 (152,276)	314,081 (80,116)	472,819 (99,109)
As percent of total E-sample population				
MER only	.55 (.07)	.36 (.10)	1.17 (.33)	1.55 (.38)
Addl dups, unadj	.43 (.08)	.63 (.16)	.37 (.20)	.56 (.27)
Total, unadj	.98 (.11)	1.00 (.18)	1.54 (.39)	2.11 (.43)
Addl dups, adj	.57 (.10)	.84 (.21)	.49 (.26)	.74 (.36)
Total, adj	1.12 (.12)	1.20 (.22)	1.66 (.43)	2.29 (.48)

Table 11 (cont.) Combining MER and duplication study results.

	30-49 Male	30-49 Female	50+ Male	50+ Female
MER only	211,016 (70,420)	47,414 (38,068)	192,607 (70,452)	213,622 (74,814)
Addl dups, unadj	170,966 (71,114)	118,977 (47,137)	140,672 (63,735)	76,096 (46,707)
Total, unadj	381,982 (99,857)	166,391 (60,491)	333,279 (107,577)	289,718 (87,480)
Addl dups, adj	225,790 (93,919)	157,130 (62,253)	185,782 (84,173)	100,498 (61,685)
Total, adj	436,806 (117,135)	204,544 (72,862)	378,389 (124,148)	314,120 (96,103)
As percent of total E-sample population				
MER only	.54 (.18)	.11 (.09)	.58 (.21)	.53 (.18)
Addl dups, unadj	.44 (.18)	.29 (.11)	.42 (.19)	.19 (.12)
Total, unadj	.98 (.25)	.40 (.15)	1.00 (.32)	.72 (.22)
Addl dups, adj	.58 (.24)	.38 (.15)	.56 (.25)	.25 (.15)
Total, adj	1.12 (.30)	.49 (.18)	1.13 (.37)	.78 (.24)

5.4 Approximate Effect on the A.C.E. Dual System Estimate

Although revised dual system estimates in full detail have not been computed to reflect the findings of Table 10, by assuming a 75.7% efficiency, the effect of the estimated 2,941,172 extra erroneous enumerations on the A.C.E. dual system estimate will exceed 3 million. Davis (2001, p. 5) summarizes the A.C.E. dual system estimate, DSE , as

$$DSE = DD \times \frac{CE}{N_e} \times \frac{N_p}{M} \quad (6)$$

where

DD = the number of census data-defined persons eligible and available for A.C.E. matching;
 CE = the estimated number of correct enumerations from the E Sample;

N_e	=	the estimated number of people from the E Sample;
N_p	=	the estimated total population from the P Sample; and
M	=	the estimated number of persons from the P-sample population who match to the census.

Although the A.C.E. applied the dual system estimator in 416 separate poststrata, collapsed from an original 448, the effect of the additional erroneous enumerations can be approximated by its effect on a single-cell dual system estimate. Nationally, $DD = 265,580,677$ and $N_e = 264,578,863$ (Feldpausch, 2001b, p. 79); the match rate $M/N_p = 91.59\%$, and the correct enumeration rate $CE/N_e = 95.28\%$ (Davis 2001, Attachment E, p. 1). Using these reported rates, the single-cell dual system estimate of the A.C.E. universe is approximately 276.28 million. If the correct enumeration rate were revised to 94.17% on the basis of the estimated 2,941,172 additional erroneous enumerations, the comparable estimate would be 273.06 million, a change of approximately 3.2 million.

6. DISCUSSION

The combined evidence from the MER/EFU review sample and the person duplication study indicates that the A.C.E. substantially underestimated erroneous enumerations. The actual effect is likely to be even greater than that estimated here, because optimistic estimates for the efficiency of computer matching were used, and this preliminary analysis was restricted to duplicates with model weights $> .98$. Furthermore, the MER data showed that the A.C.E. substantially understated some components of erroneous enumeration, and the duplicate study suggests that even the MER understates the magnitude of this understatement. The combined estimates here only use directly identified duplicates and estimates of undetected duplicates due to the efficiency of computer matching, but the results suggest that the MER could also underestimate the contribution to erroneous enumerations of persons enumerated only at the wrong residence and not duplicated.

To use this evidence to refine the A.C.E. estimates and, in turn, to adjust the census estimates for postcensal estimation will require additional research. Practically speaking, the reinterview aspect of the MER cannot be redone, but an expansion of the review subsample can be considered for clerical review in order to refine the MER/EFU review estimates used in this report.

Although beyond the scope of this report, the quality of MER data for P-sample residence could be investigated simultaneously. Reclassification of matched E-sample cases as erroneous enumerations would have implications for the P-sample estimates, and these have not yet been studied.

The large number of MER unresolved and conflicting cases leaves the findings of the MER review somewhat unclear, and a more complete analysis of the missing data is important. As noted previously, A.C.E. applied imputation rules for those with another Census Day address

when the address was not reported. The rules resulted in a high rate of imputed erroneous enumerations for these cases; a similar approach could be examined for similar unresolved EFU 2 or Best Codes.

The relatively high proportion of duplicates found among the conflicting cases in MER suggests that a high proportion of conflicting cases may represent erroneous enumerations. Further empirical evidence and analysis are required.

Because of its potential to validate and supplement the MER measurement, additional research on methods to identify person duplication now appears warranted. Further work on the Poisson model, including incorporation of the effect of middle initial, merits attention. The model can be extended from national application to matches within the same county or state. A more nuanced approach to using the Census Bureau's person matching algorithm also appears worth pursuing—the current approach measured the score produced by the algorithm against a single threshold, but then rejected many of the matches found at that threshold. The efficiency of computer matching to detect duplicates, represented here by a uniform 75.7%, requires further empirical investigation.

The estimation procedures used in this analysis easily admit of a number of refinements. Only the MER review sample is used in the analysis, ignoring the information from the rest of the A.C.E. sample. Ratio estimation to results from the person duplication study for the full A.C.E. sample could be considered, as well as other means of combining the MER and duplication information.

Childers (2001, pp. 101-102) quotes Hogan and Cowan (1980, p. 266) to describe the A.C.E. strategy for *other residence* and dual system estimation, generally. A fuller version of the quote is:

4.2.2 Determining whether someone was correctly enumerated is conceptually and operationally more difficult. One must decide not only that someone exists and should have been enumerated, but also where they should have been enumerated. The Bureau has defined two approaches:

Definition I - A person is "correctly enumerated" if he should have been enumerated and was enumerated once and only once, even though it might have been in an incorrect location. A person is "missed" if he should have been enumerated in the census but was not enumerated in any location. An enumeration is considered to be an "erroneous enumeration" if the person should not have been enumerated but was (e.g., he did not exist, lived outside the U.S., was born after the census or died before the census), or the person should have been enumerated but was enumerated more than once.

Definition II - A person is "correctly enumerated" if he was enumerated in the census at the address reported by the followup survey as the census date residence. A person is "missed" if he was not enumerated at the census date residence that was reported in the followup survey. An enumeration is considered to be "erroneous" if the followup survey reports that the person was not living at the location where the census recorded him. For example, the followup survey could report that no such person exists, or that the person was born after the census, died before the census or was living elsewhere on census date.

The Census Bureau has found that it is impossible to search all locations where a person might have been enumerated. So we are forced into Definition II. But, while seemingly clear for the purpose of defining misses, the definition must be carefully used in dealing with erroneous enumerations. In theory, where one reports one should have been enumerated should be the same regardless of how one is sampled for a followup

survey (System 2) [that is, the P-sample]. But for the people who move between the census and the followup survey, serious problems can arise. This brings us to our next issue: misstatement of address.

One of our serious problems is that many people misstate their Census Day address. Many people report that they were living “here” during the followup survey even though they have moved. A less common problem is people who report their address as “there” during the followup survey even though they moved before Census Day. This phenomenon, known as telescoping, has been uncovered in other studies with the same net result. Careful probing can reduce this problem, but it cannot eliminate it. Clearly, anyone who misstates their Census Day address will be counted as missed. This must be properly balanced in the E sample by treating people who misstate their address as erroneously enumerated. There are two ways of doing this: one potentially unbiased, but expensive, one potentially biased but cheap.

The potentially unbiased method is to followup out movers, and interview them at their new address. The interview would be a normal “System 2” survey interview. They would be asked “where they were living on Census Day”. If they correctly reported their previous address, they would be counted as correctly enumerated there. If they incorrectly reported their old address, we would treat them as erroneously enumerated at the old address. Thus, the treatment of misreporting of address is [in] the estimation of erroneous enumerations would be consistent with the estimation of omissions.

The other approach is to accept the word of the current occupant as to who was living there on Census Day. Thus, if the current occupant wrongly reports that he was living “here” on Census Day we accept this. If he also reports that the previous occupants moved out before he moved in, we accept that. Clearly, any other family enumerated in the housing unit at the time of the census was erroneously enumerated—if we accept the word of the current occupants! Again, the reports may be inaccurate but they are consistent and balancing.

The methods we have outlined are a way to handle a difficult problem. However, they do not solve the problem, and more than hot-decking has solved the problem of nonresponse.

As always, field work should be done so as to minimize nonresponse, and erroneous enumerations. Matching rules should be constructed to keep the insufficient information category as small as possible. But the problem will exist and all one can do is to attempt to handle it in an unbiased manner.

The extended passage anticipates important issues by two decades, yet unfortunately does not fully recognize additional complexities now appearing from the analysis of the MER and duplicate studies. The MER particularly indicates that a large number of persons are enumerated in both the household and group quarters population to a degree underestimated by the A.C.E. The results from the duplicate study indicate that other persons, such as children of divorced or separated parents, may be reported by respondents as members of two different households in the census, the A.C.E., and even, to a lesser degree, in the MER. Consistent reporting by respondents may have led to errors in the census almost invisible to the A.C.E. These results suggest issues to be addressed in designing both the next census and coverage measurement survey.

References

Adams, Tamara and Krejsa, Elizabeth A. (2001), “ESCAP II: Results of the Person Followup and Evaluation Followup Forms Review,” Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 24, DSSD Census 2000 Procedures and Operations Memorandum Series #T-17, Oct. 16, 2001, U.S. Census Bureau.

Bean, Susanne (2001), "ESCAP II: Accuracy and Coverage Evaluation Matching Error," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 7, Oct. 3, 2001, U.S. Census Bureau.

Byrne, Rosemary; Imel, Lynn; Ramos, Magdalena; and Stallone, Phawn (2001), "Accuracy and Coverage Evaluation: Person Interviewing Results," DSSD Census 2000 Procedures and Operations Memorandum Series B-5, Feb. 28, 2001, U.S. Census Bureau.

Cantwell, Patrick J., and Childers, Danny R. (2001) "Accuracy and Coverage Evaluation Survey: A Change to the Imputation Cells to Address Unresolved Resident and Enumeration Status," DSSD Census 2000 Procedures and Operations Memorandum Series Q-44, Mar. 6, 2001, U.S. Census Bureau.

Cantwell, Patrick J.; McGrath, David; Nguyen, Nganha; and Zelenak, Mary Frances (2001), "Accuracy and Coverage Evaluation: Missing Data Results," DSSD Census 2000 Procedures and Operations Memorandum Series B-7, Feb. 28, 2001, U.S. Census Bureau.

Childers, Danny R. (2001), "Accuracy and Coverage Evaluation: The Design Document," DSSD Census 2000 Procedures and Operations Memorandum Series, Chapter S-DT-1, Revised, Jan. 26, 2001, U.S. Census Bureau.

Davis, Peter P. (2001), "Accuracy and Coverage Evaluation: Dual System Estimation Results," DSSD Census 2000 Procedures and Operations Memorandum Series B-9, Feb. 28, 2001, U.S. Census Bureau.

Fay, Robert E. (2001), "The 2000 Housing Unit Duplication Operations and Their Effect on the Accuracy of the Population Count," presented at the Joint Statistical Meetings, Atlanta, GA, Aug. 5-9, 2001, and to appear in the *Joint Statistical Meetings 2001* on CD-ROM, American Statistical Association, Alexandria, VA. Two tables omitted from the CD version are available from the author (asa01full.pdf).

Feldpausch, Roxanne (2001a), "Census Person Duplication and the Corresponding A.C.E. Enumeration Status," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 6, DSSD Census 2000 Procedures and Operations Memorandum Series #T-16, Oct. 12, 2001, U.S. Census Bureau.

Feldpausch, Roxanne (2001b), "E-Sample Erroneous Enumeration Analysis," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 5, DSSD Census 2000 Procedures and Operations Memorandum Series #T-11, Oct. 10, 2001, U.S. Census Bureau.

Fellegi, Ivan P. and Sunter, Alan B. (1969), "A Theory for Record Linkage," *Journal of the American Statistical Association*, **64**, 1183-1210.

Hogan, Howard (1993), "The 1990 Post-Enumeration Survey: Operations and Results," *Journal of the American Statistical Association*, **88**, 1047-1060.

Hogan, Howard (2001), "Accuracy and Coverage Evaluation: Data and Analysis to Inform the ESCAP Report," DSSD Census 2000 Procedures and Operations Memorandum Series B-1, March 1, 2001, U.S. Census Bureau.

Hogan, Howard and Cowan, Charles D. (1980) "Imputations, Response Errors, and Matching in Dual System Estimation" *1980 Proceedings of the Section on Survey Research Methods*, Washington, DC: American Statistical Association, pp. 263-268.

Killion, Ruth Ann (1997), "Group Quarters and the Integrated Coverage Measurement Survey," undated U.S. Census Bureau memorandum to the Census 2000 Committee on Statistical Policy.

Krejsa, Elizabeth A. (2001), "ESCAP II: A.C.E. Erroneous Enumerations Errors: Analysis of Census Discrepant Persons," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 4, Sep. 21, 2001, U.S. Census Bureau.

Martin, Betsy (2001), "Instrument Differences and their Possible Effects: Comparison of the Evaluation Followup (EFU) and the Person Followup (PFU) Instruments," internal document, Oct. 12, 2001, U.S. Census Bureau.

Mule, Thomas (2001), "Person Duplication in Census 2000," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 20, DSSD Census 2000 Procedures and Operations Memorandum Series Q-71, Oct. 11, 2001, U.S. Census Bureau.

Nash, Fay (2000), "Overview of the Duplicate Housing Unit Operations," internal document, November 7, 2000, U.S. Census Bureau.

Prewitt, Kenneth (2000), "Accuracy and Coverage Evaluation: Statement on the Feasibility of Using Statistical Methods to Improve the Accuracy of Census 2000," , June 2000, U.S. Census Bureau.

Raglin, David A. (2001), "ESCAP II: Effect of Excluding Reinstated Census People from the A.C.E. Person Process," Executive Steering Committee on Accuracy and Coverage Evaluation Policy II, Report Number 13, Oct. 9, 2001, U.S. Census Bureau.

Robinson, J. Gregory (2001), "Accuracy and Coverage Evaluation: Demographic Analysis Results," DSSD Census 2000 Procedures and Operations Memorandum Series B-4, March 2, 2001, U.S. Census Bureau.

Sirken, Monroe G. (1972), "Stratified Sample Surveys with Multiplicity," *Journal of the American Statistical Association*, **67**, 224-227.

Smith, Annetta C. (2002), "Population in Group Quarters in Census 2000," unpublished memorandum to John F. Long, January 9, 2002, U.S. Census Bureau.

U.S. Census Bureau (1999), "Addendum to Provide Changes to the Census 2000 Residence Rules," Census 2000 Decision Memorandum No. 43, Addendum No. 2, for John H. Thompson from John F. Long, Sept. 20, 1999.

U.S. Census Bureau (2001), "Residence Rules," on World Wide Web at http://www.census.gov/population/www/censusdata/resid_rules.html, last revised Jan. 18, 2001, created Aug. 9, 1999, accessed Nov. 7, 2001. An Acrobat (.pdf) version of this page is available from the author.

Notes:

(1) Mule (2001, p.9) reports a weighted estimate of 41,046 duplicates missed clerically out of 724,687 computer matches within cluster, or about 5.7%. On the basis of the MES clerical review, Bean (2001, p. 21) obtained an unweighted estimate of missed duplicates in the A.C.E. of about 3.3%, largely offset by a 2.4% rate of false duplicates. Because standard errors were unavailable to evaluate the comparison, it is not clear whether the 5.7% rate from the duplicate study is significantly greater than the 3.3% from MES, but both estimates are small.

(2) The term *search area* appears with two related meanings in describing the A.C.E. The use here will refer to the census cluster sampled for the A.C.E. and a single ring of surrounding blocks. (For example, Feldpausch (2001a, p. iii) uses this term in the same way.) Conceptually, A.C.E. estimates of P-sample matches refer to any match 1) of whole households to census enumerations in the search area, or 2) of individual people to census enumerations in the sampled cluster. The search to surrounding blocks was targeted, however, so that surrounding blocks were searched for only a sample. Nonetheless, the A.C.E. estimates are weighted in order to represent the outcome of extended search if it had been carried out for all nonmatching households. The term *search area* can also refer operationally to the specific area to be searched: the cluster and surrounding blocks for clusters in the Targeted Extended Search sample, and only the cluster otherwise.

(3) The A.C.E. estimate was 98,335 (Table 6). A separate analysis will be required to determine to what extent the A.C.E. may have underestimated duplicates to surrounding blocks and whether this potential understatement is adequately measured by the MER estimates.

(4) As noted in Section 3, the source file for the duplication study included both *E-sample eligible housing units in the A.C.E. universe* and *reinstated housing units*, which were not in the universe. Section 2 introduces the E-sample eligible universe and A.C.E. universe; Section 3 describes reinstated housing units. Tables 2 and 6 (Mule 2000, p. 9, 11) allow the reinstated units to be partially separated out. The estimate 660,094 = 660,189 (from Table 6) - 95 (reinstated to group quarters within cluster, from Table 2). Consequently, the estimate may contain a small number of duplicates of reinstated to group quarters outside the search area. A similar problem affects Table 5 here.

(5) For example, approximately 5.8M census enumerations were recorded with so few population characteristics that all of their population characteristics were imputed. Such whole person imputations were not eligible for the E sample. Census reinstated cases, described in Section 3, were also ineligible. The E sample was used to measure the category *persons with insufficient information for matching*, who were persons who were considered "data-defined" by the presence of sufficient information by census

standards (and therefore not included among the 5.8M with all characteristics imputed). This category included persons with incomplete name, such as no first name. Matches of P-sample cases to census enumerations with insufficient information for matching were not allowed. Generally, only E-sample eligible cases were considered for purposes of P-sample matching, but matches from the P sample to census enumerations of group quarters were allowed (Childers 2001, p. 1).

(6) Mule (2001) showed that the decline in *duplicates* from 1990 could largely be attributed to the effect of the Housing Unit Duplication Operations, which permanently removed some preliminary census enumerations that appeared to be duplicate housing units and isolated other units, the reinstated cases, from the A.C.E. universe. (The reinstated cases were included in the final census.) Krejsa (2001) found no significant error in the estimation of *fictitious*. The change in *geocoding* was small and also was investigated with the MER. There were some changes in the standards for *insufficient information* between 1990 and 2000 (Feldpausch 2001b, p. 16). The identification of cases as *insufficient information* was governed by rules that could have been implemented clerically without expected difficulty. The MER study allowed reclassification of cases by reapplying the definition, and a small number of cases were reclassified in this way, primary reclassifying some cases out of *insufficient information* into some other status (personal communication, Susanne Bean, Oct. 19, 2001). The effect is included in MES estimates (Bean 2001) but not separately identified.

(7) Martin (2001, p. 6) identifies situations for which EFU did not obtain addresses: 1) person died after Census Day/stayed at another residence on Census Day, 2) person never lived at sample address, 3) college student stayed at another housing unit on April 1, 4) person moved out before April 1 or in after April 1. She also noted that the EFU did not resolve which residence was correct for persons living in group quarters where persons are allowed to indicate their usual home is elsewhere. These group quarters include, for example, military barracks or ships, but not college dormitories or nursing homes.

(8) Martin (2001, pp. 1-2) states "It is important to note that interviewers in the Person Followup and the Evaluation Followup were instructed to write notes, and these notes (as well as other auxiliary information) were used heavily in classifying match codes. Even if information would seem to be lacking because there is no pertinent question, it may be available in notes obtained by well-trained interviewers. However, as a rule notes would be considered to provide less reliable and uniform data than [than] responses to standardized survey questions."

(9) The codes were for both the cases sent to person followup (PFU) and those cases not sent, almost all of which were matches to the census. Adams and Krejsa (2001) use the term *PFU 1* to apply to both sets of cases, although the acronym suggests the person followup only.

(10) Besides *group quarters*, Table 3 (Adams and Krejsa 2001, p. 9) includes the categories *movers* (primarily those who would have moved in after Census Day), *never lived here*, *address mixup*, *birth or death*, *other residence--interview at first home*, *other residence--interview at second home*, and *other residence--unspecified*, which all pertain to *other residence* issues. Persons born after or dying before Census Day are included in the broad category of *other residence*; the estimate 39,395 (Table 3) indicates that this issue is at most a small component of the underestimation of erroneous enumerations in the E sample. Table 3 does not provide more detail on 76,262 classified as *other*; in fact, some or all may be categorized as *other residence* rather than *fictitious* or *geocoding error*.

(11) Hogan (1993, p. 1056) remarks on the group "other counting errors" which are essentially equivalent to *other residence*: "Most of the 'other counting errors' are enumerations of people who moved into the address after Census Day. If they were missed at the correct location, then this may be the only place that they were enumerated. This type of error is often, but not always, paired with census omissions of the actual Census Day residents."

(12) The first phase in effect completed the definition of the A.C.E. universe, because any housing unit tentatively removed during the first phase was removed. The first phase was completed in time for the start of A.C.E. matching in Oct. 2000. The second phase was not completed until November (Nash 2000).

(13) Most links were pairs. The generalization of the rules to more than two matches retained a single unit in the A.C.E. universe and provisionally removed the rest. In determining the unit to retain, an occupied unit was selected over a vacant one, the unit with more persons was selected, or when the number of persons was equal, the earlier or more completely recorded unit was selected (Nash 2000 and material it cites).

(14) Matching 1) allowed for reversal of first and last name, 2) removed "Jr," "Sr," and "III" from first and last name fields, 3) located middle initials at the end of names such as "SMITHL" and 4) allowed a match of year within one year (Mule 2001, p. 4, App. B).

(15) Most but not all of these names were Spanish; Patrick on March 17 is a familiar non-Spanish example (Mule 2001, App. H). Instances of "John Doe" or "Jane Doe" were also eliminated, as were name/birth date combinations used in census training manuals (Mule 2001, pp. J-2 to J-3).

(16) For purposes of replication, the unrounded value of .75718900, based on an earlier version of Table 6, is included in subsequent calculations. The parallel calculation with the values in Table 6 gives .75719059.

(17) Because Mule (2001) employed this weight in his analysis, the omission from the calculation is unexpected. But recalculation with the weight from the Poisson model reduces values in Table 7 by less than 10%.

(18) It is possible that in some cases the enumeration in the group quarters is erroneous and that the person should have been enumerated as part the E-sample household, but this explanation seems unlikely to occur frequently for the major types of duplicates, such as dormitories and nursing homes, (Feldpausch 2001a, Table 2, p. 5).

(19) Census residence rules are posted on the Census Bureau's web site (U.S. Census Bureau 2001), where 11 different categories of living situations are discussed separately (People Away on Vacation or Business, People Without Housing, People With Multiple Residences, ...). The official source (U.S. Census Bureau 1999) provides 31 rules. These two sources appear to contradict each other on a few points and even to be possibly internally inconsistent. As one example, a member of the military who lives most of the time in barracks but lives in a household on April 1 appears to be directed to be counted onbase according to the rules on the web site but apparently is covered by Rule 4 (U.S. Census Bureau 1999) to live offbase.

(20) A key summary of the design (Prewitt 2000) omits this point. Childers (2001) documents operational aspects of the interaction between the A.C.E. and the group quarters population, but does not present evidence on the quality of the count for group quarters. Hogan (2001, p. 57) noted "The A.C.E. universe differed from that of the PES. The A.C.E. excluded the noninstitutional nonmilitary group quarters, while the 1990 PES had included this group. The A.C.E. DSE implicitly attributes zero coverage error to this group. The PES DSE attempted to measure the coverage of this group. However, there is no evidence that this coverage of this group was so very far from correct as to explain much of the PES/A.C.E. error of closure." The text does not appear to indicate what evidence was reviewed, but the implicit citation may be to Robinson (2001, p. 8), who provides somewhat more detail. "Second, we compared rough benchmarks of the GQ population by type (e.g., correctional institutions, nursing homes, military quarters, college dormitories) to Census 2000 results to broadly assess coverage completeness of GQs. The benchmarks of the GQ population generally agree with the Census 2000 results."

(21) A few MER records matched to more than one duplicate record. A single duplicate record was selected, with preference for E-sample eligible units first and then for group quarters. Within each type, the record with the highest model weight was chosen.

(22) The weights are related to probabilities, and $\text{weight} > .98$ is used to identify almost certain duplications. For common names, however, where coincidental sharing of birthday is more frequent than census duplications, the weights can be negative and are typically closer to 0 than to 1. To the extent that the weights can be used effectively as probabilities for most names, then introduction of the weights into the analysis could be based on a modification to eq. (5), estimating the first term on the right-hand side with the weights, but omitting the weights in calculating the remaining terms that are subtracted.